

(4)

11. Trace the curve $y^2 = (x-1)(x-2)(x-3)$. 15

12. (a) If $I_n = \int_0^{\pi/4} \tan^n x dx$; prove that $I_{n-1} + I_{n+1} = \frac{1}{n}$.
Deduce the value of I_5 . 10

(b) Evaluate $\int \frac{xe^x}{(x+1)^2} dx$. 5

13. If $y = \sin(m \sin^{-1} x)$, $|x| < 1$; prove that :

(a) $(1-x^2)y_2 - xy_1 + m^2y = 0$ 5

(b) $(1-x^2)y_{n+2} - (2n+1)xy_{n+1} + (m^2 - n^2)y_n = 0$
and find value of $y_n(0)$. 10

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BCA-I Sem.

Roll No.

18005

B. C. A. Examination, Dec. 2016

MATHEMATICS-I

(BCA-101)

(New Course)

Time : Three Hours]

[Maximum Marks : 75

Note : Attempt questions from all Sections as per instructions.

Section-A

(Very Short Answer Questions)

Attempt all the five questions of this Section.

Each question carries 3 marks. Very short answer is required. $3 \times 5 = 15$

1. Show that $A = \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix}$ is nilpotent matrix of order 2. 3

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(2)

2. If $y = \log[\log(\log x)]$, find $\frac{dy}{dx}$. 3

3. Evaluate $\int \frac{(a^x - b^x)^2}{a^x b^x} dx$. 3

4. Calculate the area of parallelogram spanned by the vectors $a = (3, -3, 1)$ and $b = (4, 9, 2)$. 3

5. Evaluate $\lim_{n \rightarrow \infty} \frac{\sum n^2}{n^3}$. 3

Section-B

(Short Answer Questions)

Attempt any *two* questions out of the following three questions. Each question carries $7\frac{1}{2}$ marks. Short answer is required. $7\frac{1}{2} \times 2 = 15$

6. Find the rank of the matrix $\begin{bmatrix} 1 & 2 & 3 & 2 \\ 2 & 3 & 5 & 1 \\ 1 & 3 & 4 & 5 \end{bmatrix}$. $7\frac{1}{2}$

7. Evaluate $\int \frac{3x+1}{(x-1)^2(x+3)} dx$. $7\frac{1}{2}$

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8. Expand $\sin x$ in power of x and hence find $\sin 18^\circ$ upto four decimal places. $7\frac{1}{2}$

Section-C

(Detailed Answer Questions)

Attempt any *three* questions out of the following five questions. Each question carries 15 marks. Answer is required in detail. $15 \times 3 = 45$

9. (a) Show that $\lim_{x \rightarrow 0} \frac{e^{1/x} - 1}{e^{1/x} + 1}$ does not exist. 5

(b) Examine the continuity of the function at the indicated point. Also point out the type of discontinuity; if any : 10

$$f(x) = \begin{cases} \frac{e^{1/x} - e^{-1/x}}{e^{1/x} + e^{-1/x}} & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$$

10. Verify Cayley-Hamilton theorem for the matrix :

$$A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$$

and hence find A^{-1} . Also state the Cayley-Hamilton theorem. 15

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10. Examine the continuity of the function:

$$f(x) = \begin{cases} -x^2 & \text{if } x \leq 0 \\ 5x - 4 & \text{if } 0 < x \leq 1 \\ 4x^2 - 3x & \text{if } 1 < x < 2 \\ 3x + 4 & \text{if } x \geq 2 \end{cases}$$

at $x=0, 1$ & 2 . 15

11. Trace the curve $x^3 + y^3 = 3axy$. 15

12. (i) Expand $\log(1+x)$ by Maclaurin's Theorem. 15

(ii) Expand $\sin x$ in powers of $(x-\pi/2)$ by using Taylor's Theorem. 15

13. Evaluate :

(i) $\int \frac{e^x(1+x)}{\cos^2(e^x x)} dx$

(ii) $\int \sin x \sin 2x \sin 3x dx$

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Roll No.....

BCA-I Sem.

18005

B.C.A. Examination, Dec. 2017

MATHEMATICS-I

(BCA-101)

(New Course)

Time : Three Hours]

[Maximum Marks : 75

Note : Attempt questions from **all** sections as per instructions.

Section-A

(Very Short Answer Questions)

Note : Attempt all the **five** questions of this section. Each question carries **3** marks. Very short answer is required. $3 \times 5 = 15$

1. Show that $A = \begin{bmatrix} 1 & 1-i & 2 \\ 1+i & 3 & i \\ 2 & -i & 0 \end{bmatrix}$ is Hermitian.

3

P.T.O.

(54)

2. Define continuity of a function at a point. 3
3. Show that the parabola $y^2 - 4ax = 0$ has no asymptote. 3
4. Define Gamma and Beta function. 3
5. Define vector in 3-dimensions with example. 3

Section-B

(Short Answer Questions)

Note : Attempt any **two** questions out of the following **three** questions. Each question carries $7\frac{1}{2}$ marks. Short answer is required. $7\frac{1}{2} \times 2 = 15$

6. A function $f(x)$ is defined as follows:

$$f(x) = \begin{cases} (x^2/a) - a, & \text{when } x < a \\ 0, & \text{when } x = a \\ a - (a^2/x), & \text{when } x > a \end{cases}$$

Prove that the function $f(x)$ is continuous at $x=a$.

7. Find n^{th} differential coefficient of $x^3 \cos x$.

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8. Find the area of a rectangle having vertices A, B, C & D with position vectors.

$$a = \left(-1, \frac{1}{2}, 4\right), b = \left(1, \frac{1}{2}, 4\right)$$

$$c = \left(1, \frac{-1}{2}, 4\right), d = \left(-1, \frac{-1}{2}, 4\right)$$

respectively.

Section-C

(Detailed Answer Questions)

Note : Answer any **three** questions out of the following **five** questions. Each question carries **15** marks. Answer is required in detail. $15 \times 3 = 45$

9. Verify Cayley-Hamilton theorem 15

$$A = \begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$$

Also determine the characteristic roots and corresponding characteristic vector of the matrix A.

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P.T.O.

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(4)

10. Check the continuity of the following functions at

$x=0$:

(i) $f(x) = \frac{|x|}{x}$ for $x \neq 0$ and $f(0) = 0$

(ii) $f(x) = \frac{e^{1/x} \sin(1/x)}{1+e^{1/x}}$ for $x \neq 0$ and $f(0) = 0$.

11. Trace the curve $9ay^2 = (x-2a)(x-5a)^2$.

12. (i) Expand $\frac{e^x}{e^x+1}$ by Maclaurin's theorem.

(ii) Expand $\log x$ in power of $(x-1)$ by Taylor's theorem.

13. Evaluate :

(i) $\int \tan^4 x \, dx$

(ii) $\int \frac{\cos 2x - \cos 2\alpha}{\cos x - \cos \alpha} dx$.

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BCA-I Sem.

Roll No.

18005

B. C. A. Examination, Dec. 2018

MATHEMATICS-I

(BCA-101)

(New Course)

Time : Three Hours]

[Maximum Marks : 75

Note : Attempt questions from all Sections as per instructions.

Section-A

(Very Short Answer Questions)

Attempt all the five questions. Each question carries 3 marks. Very short answer is required.

3×5=15

1. Show that $A = \begin{bmatrix} 3 & 1+2i \\ 1-2i & 2 \end{bmatrix}$ is Hermitian.

2. Define limit of a function at a point.

(2)

- Find the asymptotes of the curve $\frac{a^2}{x^2} - \frac{b^2}{y^2} = 1$.
- State fundamental theorem of calculus.
- Define vector in 2-dimension with example.

Section-B

(Short Answer Questions)

Attempt any *two* questions out of the following three questions. Each question carries $7\frac{1}{2}$ marks.

Short answer is required. $7\frac{1}{2} \times 2 = 15$

- Determine the values of a, b, c for which the function :

$$f(x) = \begin{cases} \frac{\sin(a+1)x + \sin x}{x} & \text{for } x < 0 \\ c & \text{for } x = 0 \\ \frac{(x+bx^2)^{1/2} - x^{1/2}}{bx^{3/2}} & \text{for } x > 0 \end{cases}$$

is continuous at $x = 0$.

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(3)

- If $y = a \cos(\log x) + b \sin(\log x)$, show that :
 $x^2 y_2 + xy_1 + y = 0$ and $x^2 y_{n+2} + (2n+1)xy_{n+1} + (n^2+1)y_n = 0$.
- Calculate the area of parallelogram spanned by the vectors $a = (1, -1, 3)$ and $b = (2, -7, 1)$.

Section-C

(Detailed Answer Questions)

Attempt any *three* questions out of the following five questions. Each question carries 15 marks.

Answer is required in detail. $15 \times 3 = 45$

- Verify Cayley-Hamilton theorem for the matrix :

$$A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$$

Also determine the characteristic roots and corresponding characteristic vector of the matrix A .

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13. (i) Find the Rank of the matrix

$$A = \begin{bmatrix} 2 & 2 & 2 \\ 2 & 2 & 2 \\ 2 & 2 & 2 \end{bmatrix}$$

(ii) Find the adjoint of the matrix

$$A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$$

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BCA-I Sem.

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Roll No.

18005

B.C.A. Examination, November 2019

MATHEMATICS-I

(BCA-101)

Time : Three Hours]

[Maximum Marks : 75

Note : Attempt questions from all Sections as per instructions.

Section-A

Note : Attempt all the five question of this section. Each question carries 3 marks. Veryshort answer is required. 5×3=15

1. Define rank of a matrix.
2. Show that $\lim_{x \rightarrow 2} \frac{|x-2|}{x-2}$ does not exist.
3. Verify Rolle's theorem for the function.

$$f(x) = 2x^3 + x^2 - 4x - 2, \quad x \in [-\sqrt{2}, \sqrt{2}]$$

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[P.T.O.]

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4. Evaluate:

$$\int x^2 e^x dx$$

5. Write the formula of $\vec{a} \cdot \vec{b}$ and $\vec{a} \times \vec{b}$.

Section-B

Note : Attempt any two questions out of the following three questions. Each question carries $7\frac{1}{2}$ marks. Short answer is required.

$$2 \times 7\frac{1}{2} = 15$$

6. Solve the following system of equations by Cramers Rule

$$3x + 4y = 5$$

$$x - y = -3$$

7. Differentiate $(\sin x)^x$

8. Evaluate:

$$\int \frac{xe^x}{(1+x)^2} dx$$

Section-C

Note : Answer any three questions out of the following five questions. Each question carries 15 marks. Answer is required in detail.

$$3 \times 15 = 45$$

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9. (i) Given:

$$\vec{a} = \hat{i} + 3\hat{j} - 2\hat{k}$$

$$\vec{b} = -\hat{i} + 3\hat{k}$$

Find $\vec{a} \cdot \vec{b}$ and $|\vec{a} \times \vec{b}|$

(ii) Find the unit vector perpendicular to both the vectors

$$4\hat{i} - \hat{j} + 3\hat{k} \text{ and } -2\hat{i} + \hat{j} - 2\hat{k}$$

10. Evaluate the following Integral of limit of sum

$$\int_a^b x dx.$$

11. Evaluate by L' Hospital rule

(i) $\lim_{x \rightarrow 1} \frac{x^5 - 2x^3 - 4x^2 + 9x - 4}{x^4 - 2x^3 + 2x - 1}$

(ii) $\lim_{x \rightarrow 0} \frac{x - \sin x}{x^3}$

12. (i) Evaluate $\lim_{x \rightarrow 0} \frac{x - |x|}{x}$

(ii) Given $f(x) = \frac{|x|}{x}$, for $x \neq 0$

and $f(0) = 0$

show that $f(x)$ is not continuous at $x = 0$

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[P.T.O.]

4. Give the statement of Rolle's theorem.
5. In short, explain Dot product and Cross product.

Section-B

Note : Attempt any **two** questions out of the three questions. Each question carries $7\frac{1}{2}$ marks. $2 \times 7\frac{1}{2} = 15$

6. Solve the following equations by Cramer's Rule

$$3x + 4y = 5$$

$$x - y = -3$$

7. Use Maclaurin's theorem to prove that

$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots \dots \dots (-1)^{n/2} \frac{x^n}{n!} + \dots$$

8. If $I_n = \int_0^{\pi/3} \tan^n x dx$ then show that $(n-1)$

$$(I_n + I_{n-2}) = (\sqrt{3})^{n-1}$$

Section-C

Note : Attempt any **three** questions out of the following five questions. Each question carries 15 marks. $3 \times 15 = 45$

9. What do you mean by L-Hospital rule? Evaluate $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\log(x - \frac{\pi}{2})}{\tan x}$ by using L-Hospital Rule.

10. Examine the function $f(x)$ given by $f(x) = 10x^6 - 24x^5 + 15x^4 - 40x^3 + 108$ for maximum and minimum values.

11. If $\vec{F} = (x^2 + y^2)\hat{i} - 2xy\hat{j}$ and curve C is the rectangle in xy-plane bounded by $y=0$, $x=a$, $y=b$, $x=0$ then prove that

$$\int_C \vec{F} \cdot d\vec{r} = -2ab^2$$

12. If $f(x) = \frac{|x|}{x}$, for $x \neq 0$

and $f(x) = 0$, for $x = 0$

then show that $f(x)$ is not continuous at $x = 0$.

13. Investigate for what values of λ, μ the simultaneous equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

Prove (i) no solution (ii) a unique solution

and (iii) infinitely many solutions.

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BCA-I Sem.

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Roll No.

18005

B.C.A. Examination, Dec.-2020

MATHEMATICS-I

(BCA-101)

Time : Three Hours]

[Maximum Marks : 75

Note : Attempt questions from all sections
as per instructions.

Section-A

Note : Attempt all the five questions of
this section. Each question carries 3
marks. $5 \times 3 = 15$

1. Define rank of a Matrix with example.
2. Find third differential coefficient of $x^4 \cdot e^{2x}$.
3. What do you mean by Beta and Gamma function?

P.T.O.